

1 Fault Tolerant Shape Formation in the Amoebot 2 Model

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7 Abstract

8 The amoebot model is a distributed computing model of programmable matter. It envisions
9 programmable matter as a collection of computational units called amoebots or particles
10 that utilize local interactions to achieve tasks of coordination, movement and conformation.
11 In the geometric amoebot model the particles operate on a hexagonal tessellation of the
12 plane. Within this model, numerous problems such as leader election, shape formation or
13 object coating have been studied. One area that has not received much attention so far, but
14 is highly relevant for a practical implementation of programmable matter, is fault-tolerance.
15 The existing literature on that aspect allows particles to crash but assumes that crashed
16 particles do not recover. We propose a new model in which a crash causes the memory
17 of a particle to be reset and a crashed particle can detect that it has crashed and try to
18 recover using its local information and communication capabilities. We propose an algorithm
19 that solves the hexagon shape formation problem in our model if a finite number of crashes
20 occur and a designated leader particle does not fail. At the heart of our solution lies a
21 fault-tolerant implementation of the spanning forest primitive, which, since other algorithms
22 in the amoebot model also make use of it, is also of general interest.

23 **Model extension** In our work we extend the *geometric amoebot model* (introduced in [1])
24 by the aspect of fault-tolerance and, in order to gain initial insights, focus on the problem of
25 shape formation using the hexagon shape formation problem as basis. We extend the model
26 by introducing *particle crashes*. We assume that the adversarial scheduler may arbitrarily
27 crash particles. A crash of a particle p has the following effects: The scheduler sets the *state*
28 in p 's local memory to `CRASHED` and may arbitrarily change the rest of p 's local memory.
29 This means that p and its neighbours can reliably detect that it has crashed, the rest of p 's
30 local memory, however, is no longer reliable. Particles can then try to recover using their
31 local communication capabilities.

32 **Problem description** For any two nodes $u, v \in V_\Delta$ the *distance* $\delta(u, v) \in \mathbb{N}_0$ between u
33 and v is defined as the length of a shortest path from u to v in G_Δ . For a node $v \in V_\Delta$ and
34 $i \in \mathbb{N}_0$ let $B(v, i) := \{ u \in V_\Delta \mid \delta(u, v) = i \}$. We call a set $V \subseteq V_\Delta$ a *hexagon with centre*
35 $v \in V$ if there $k \in \mathbb{N}_0$ and a subset $S \subseteq B(v, k)$ such that $V = S \cup \bigcup_{i < k} B(v, i)$. We define
36 the *hexagon shape formation problem* **HEX**: We assume that the system of particles initially
37 forms a single connected component of contracted particles, has a unique leader, called the
38 `SEED` particle, and that all other particles are `IDLE`. The goal is to reach a stable configuration
39 in which the set of nodes occupied by particles is a hexagon with the `SEED` in its centre.

40 **Main results** We propose an algorithm **HexagonFT** that solves the hexagon shape formation
41 problem **HEX** in our model under the presence of particle crashes. Our two main results are:

42 ▶ **Lemma 1.** *If a finite number of crashes occur during the execution of algorithm HexagonFT*
43 *and m particles are faulty after the last crash, then a non-faulty configuration is reached*
44 *within $\mathcal{O}(mn)$ rounds after the last crash.*

45 ▶ **Theorem 2.** *If a finite number of crashes occur, then the algorithm HexagonFT solves the*
46 *hexagon shape formation problem HEX in worst-case $\mathcal{O}(n^2)$ work (total number of moves*



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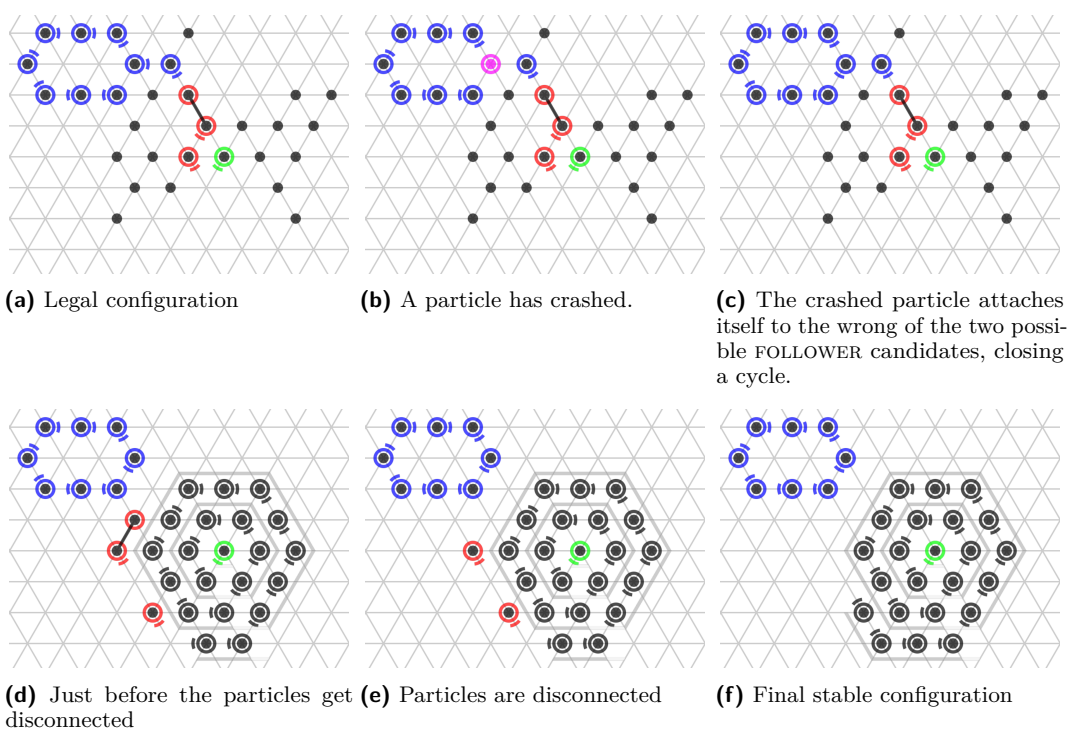
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47 *executed by all particles*). From the time when no more crashes occur and the configuration
48 *is non-faulty*, the algorithm needs $\mathcal{O}(n)$ rounds until termination.

49 **Illustration** Our fault-tolerant solution builds upon two primitives, a *propagation primitive*
50 and a *safety primitive*, each of which solves a significant problem: Firstly, we need to
51 ensure that when a crashed particle chooses a FOLLOWER as parent, this does not lead to
52 disconnection of the particles (see Figure 1). In order to avoid disconnection, we use a
53 validation mechanism that determines for a faulty particle which of the FOLLOWER parent
54 candidates it can attach to without closing a cycle. Secondly, we must ensure that particles
55 within the hexagon shape formed so far do not leave it at any time. If this is not ensured,
56 various problematic consequences are possible: among other things, the particles may be
57 disconnected, it is not guaranteed that a hexagon will be built, and it is even possible that
58 the algorithm will no longer terminate.



■ **Figure 1** The figure shows that if a crashed particle attaches itself to a arbitrary FOLLOWER pointing away from it, this can lead to irreversible disconnection of the particles.

59 — References —

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